



An efficient certificat-less key management architecture

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- 1 Introduction
- 2 Public key infrastructure (PKI)
- 3 Identity based cryptography
- 4 The proposed solution
- 5 To summarize

A key management architecture refers to the technical mechanisms, procedures and policies that collectively provide a secure network environment. It provides the following services :

- Authentication
- Confidentiality
- Integrity
- Non-Repudiation

A key management architecture is composed of 4 phases :

- **The enrollment phase** : registration of the users belonging to the concerned group, and the initial distribution of private and public keys ;
- **The re-keying phase** : re-initialization of all private keys periodically ;
- **The communication phase** ;
- **The revocation phase** : revoked user doesn't belong anymore to the group.

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There are 2 types of architectures :

- Certificate based infrastructures (RSA, ElGamal, ...);
- Certificat-less infrastructure (identity based cryptography).

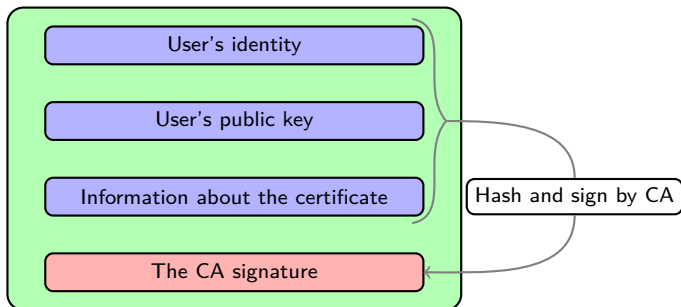
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- 2 Public key infrastructure (PKI)**
 - The enrollment/rekeying phase
 - The communication Phase
 - PKI weaknesses
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PKI

Public key infrastructure is a certificate based key management architecture, and it use 2 core elements ; Public Key Cryptography and Certification Authorities.

A certificate

A certificate is an electronic document used to prove ownership of a public key.



The components of a certificate

Usually a PKI is composed of 3 authorities :

- Registration authority (RA);
- Certificate authority (CA);
- Validation authority (VA).

Other services :

- Directory service (DS);
- Certificate revocation list (CRL).



FIGURE: The enrollment/rekeying phase of a PKI

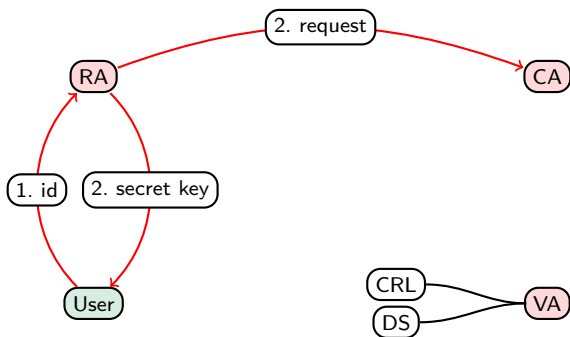


FIGURE: The enrollment/rekeying phase of a PKI

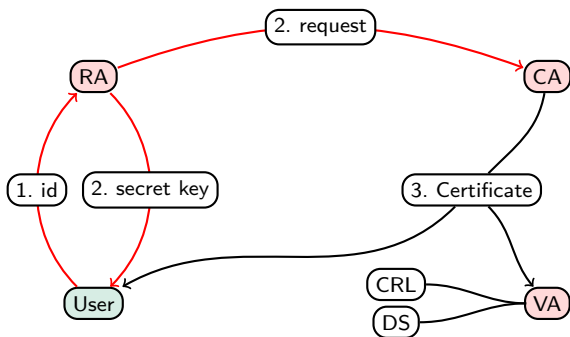


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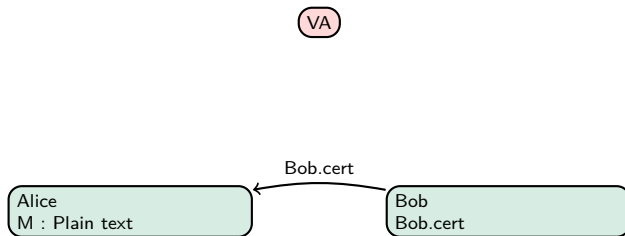


FIGURE: The communication phase of PKI

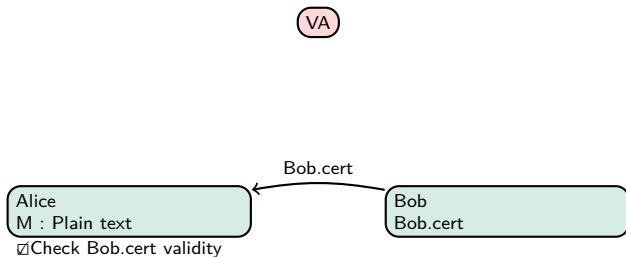


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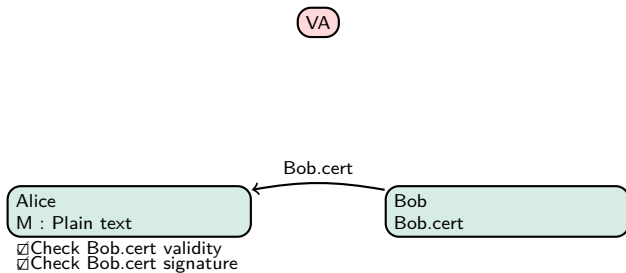


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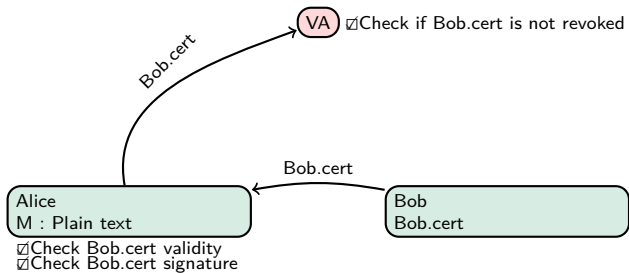


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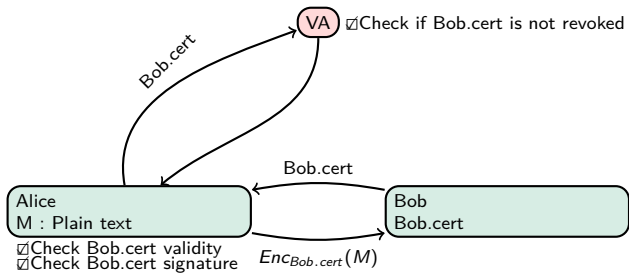


FIGURE: The communication phase of PKI

PKI weaknesses

- Revoked certificates must be stored in a certificate revocation list (CRL) ;
- Secret key is not generated by the user ;
- The CA can sign a fake certificates ;
- Enrolment and rekeying needs to be done via a private channel ;
- The secret keys are not protected.

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 - IBE communication phase
 - advantages and disadvantages
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- Identity based cryptography was introduced as an open problem by Adi Shamir in 1984 ;
- In 2001 Boneh and Franklin presented an effective IBE based on the bilinear Diffie-Hellman problem ;
- B.F IBE is composed of one authority called PKG (Private Key Generator) that generate/update users keys ;
- The user public key is a hash of his identity ;
- The PKG can calculate users secret keys by using his secret key and the user's identity.

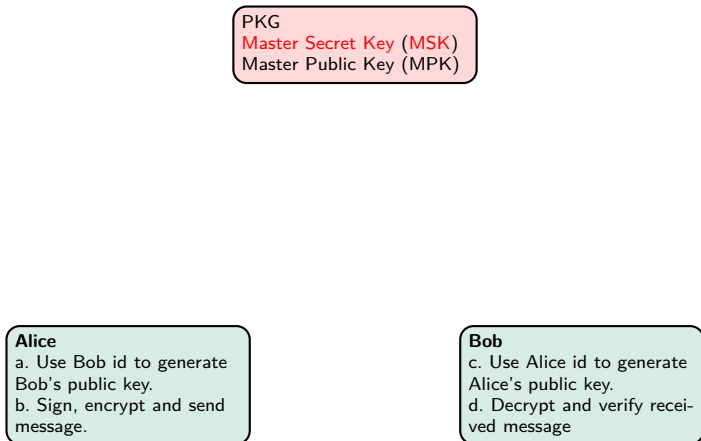


FIGURE: The communication phase in B.F IBE

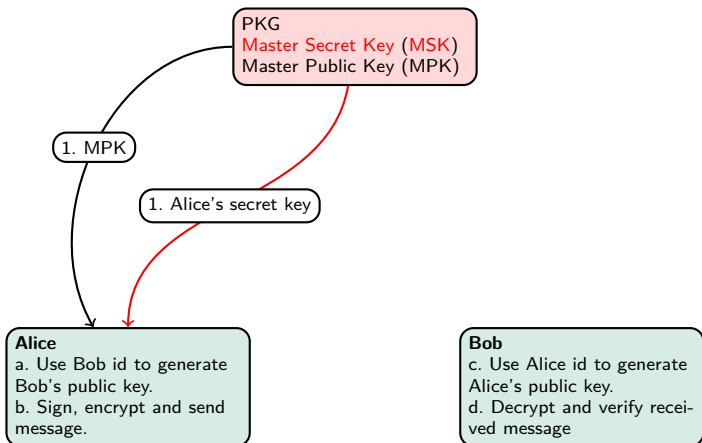


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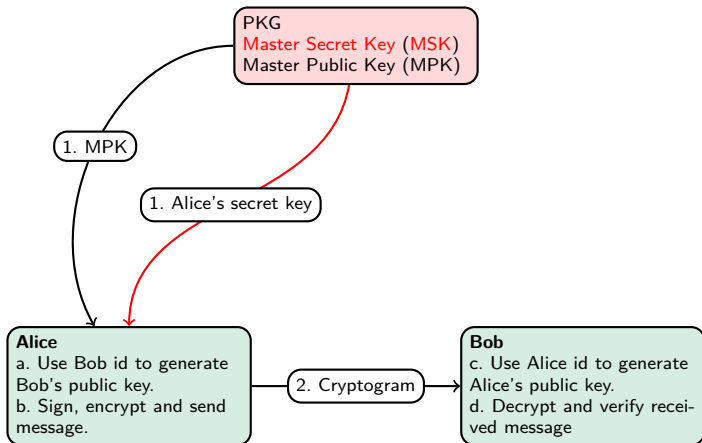


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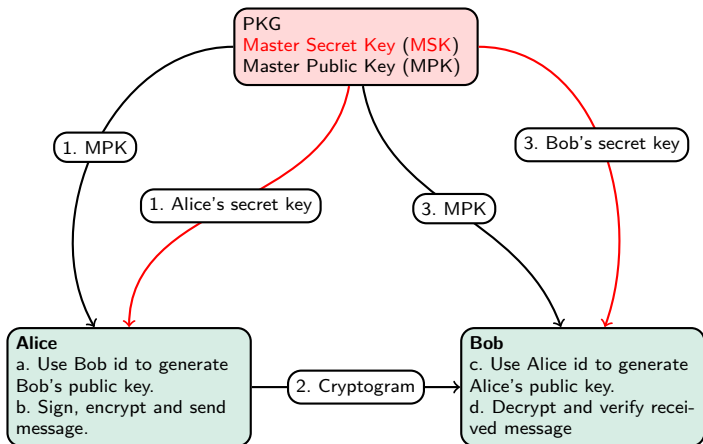


FIGURE: The communication phase in B.F IBE

advantages/ disadvantages

Advantages :

- It doesn't require a CRL to revoke entities ;
- It solves the authentication problem, (no certificates) ;
- A user doesn't need to store his private key.

Disadvantages :

- The system's security is based on a single entity : the PKG ;
- PKG interfere in each communication to provide the secret key, it may slow down the network ;
- The distribution have to be done over a private channel.

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 - The rekeying phase
 - The revocation phase
 - The communication phase
 - The hierarchical model
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We want :

- A flexible system regarding the key escrow (law, needs, security policy) ;
- Many authorities that collectively calculate the user's secret key (Lee et al.[5]) ;
- Only the user can construct his secret key (Sattam and Paterson [1]) ;
- A real time revocation that does not depend of a CRL ;
- No list of public keys ;
- Possibility to encrypt a file that could be decrypted only in future.

- We use the **Barreto-Naehring elliptic curves with optimal Ate pairing** ;
- $\mathbb{G}_0, \mathbb{G}_1, \mathbb{G}_T$ three groups with prime order q ;
- The optimal Ate pairing is a bilinear function $e : \mathbb{G}_0 \times \mathbb{G}_1 \rightarrow \mathbb{G}_T$;
- $\forall a, b \in \mathbb{Z}_q, P, Q \in \mathbb{G}_0 \times \mathbb{G}_1$ we have :

$$e(aP, bQ) = e(abP, Q) = e(P, abQ) = e(P, Q)^{ab} \in \mathbb{G}_T \quad (1)$$

- we use two authorities (at least) :
 - ▶ Static PKG : is an off-line server that contributes only during the enrollment phase ;
 - ▶ Dynamic PKG : is an on-line server that participate in the construction of the user's secret key, keys update.

PKG_{st} S.K : $s_0 \in \mathbb{Z}_q^*$ P.K : $P_0 = s_0 P \in \mathbb{G}_0$ $Y = s_0 s_1 P$ PKG_{dy} S.K : $s_1 \in \mathbb{Z}_q^*$ P.K 1 : $P_1 = s_1 P \in \mathbb{G}_0$ P.K 2 : $P'_1 = s_1 P' \in \mathbb{G}_1$ **Bob**P.K : $Q_B = \mathcal{H}_1(id_B)$

FIGURE: The enrollment phase in IBE-2

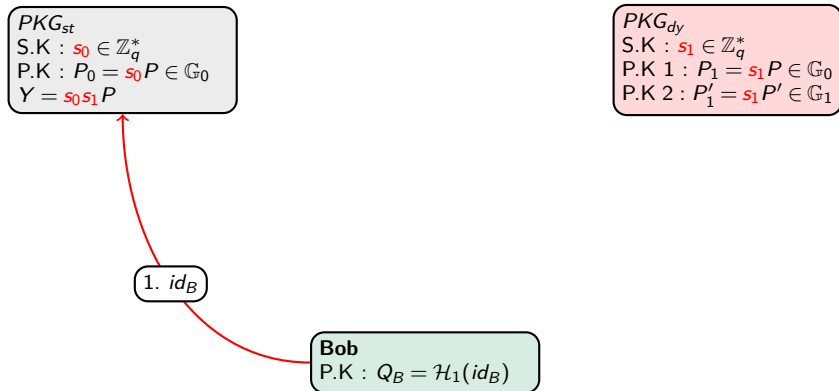


FIGURE: The enrollment phase in IBE-2

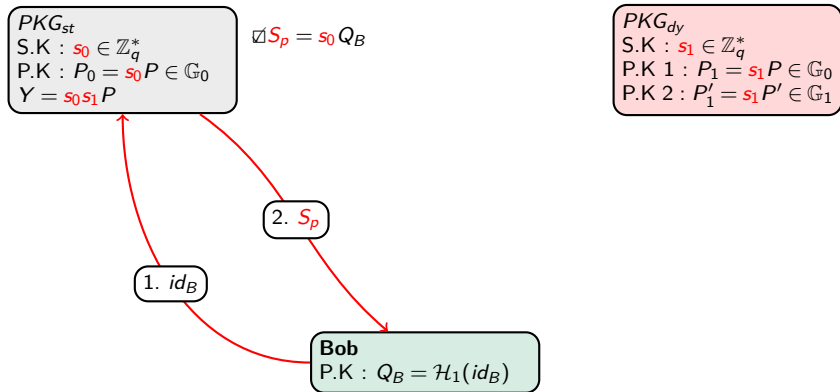


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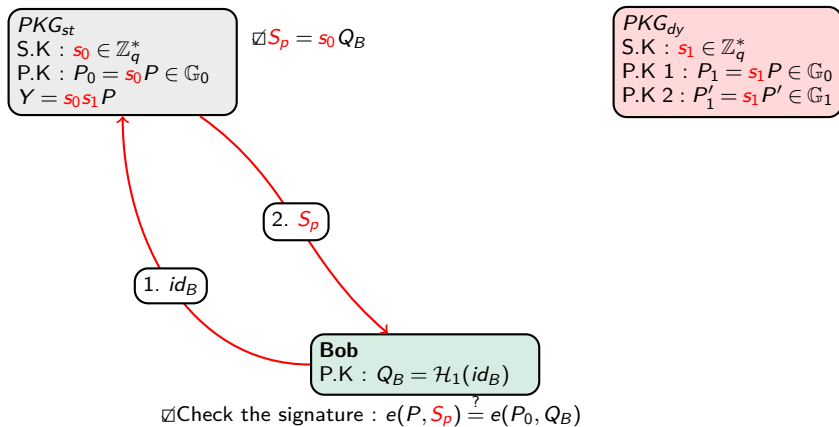


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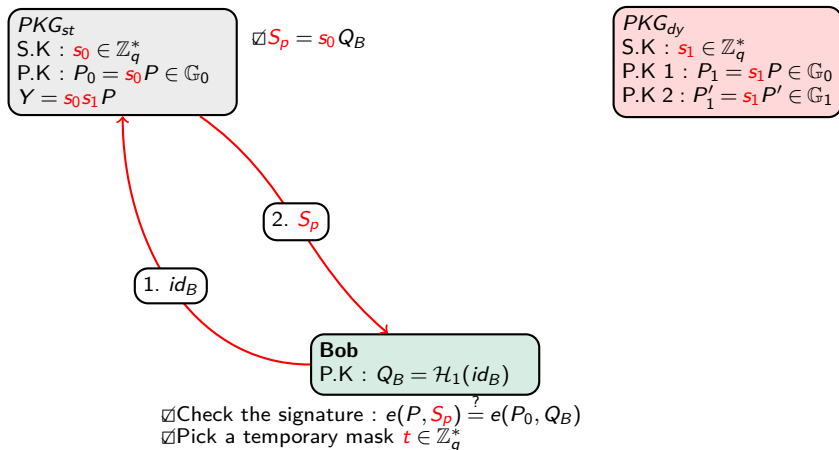


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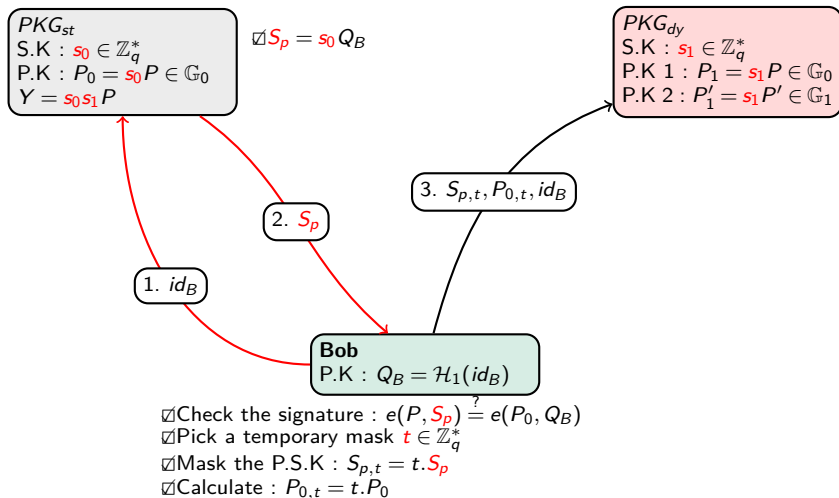


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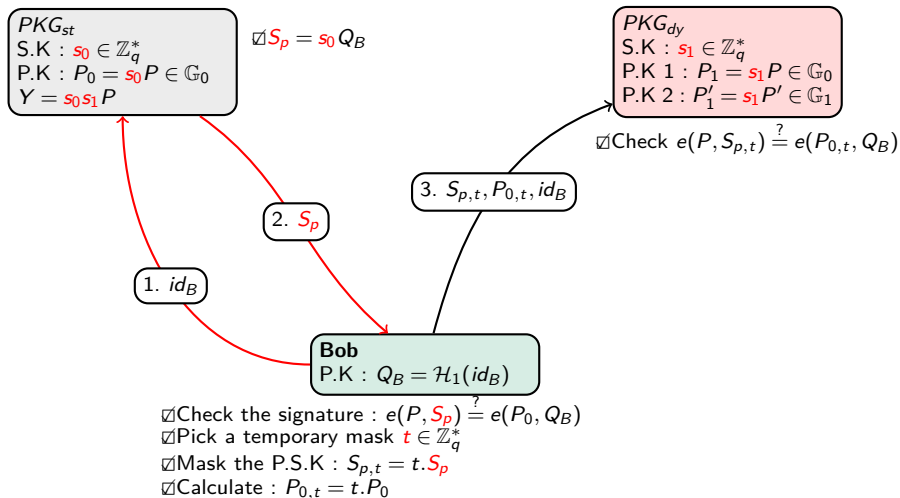


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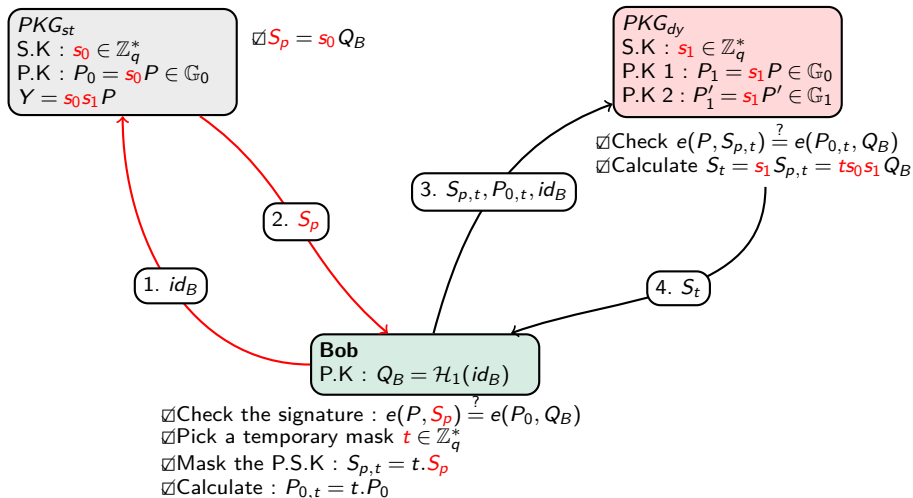


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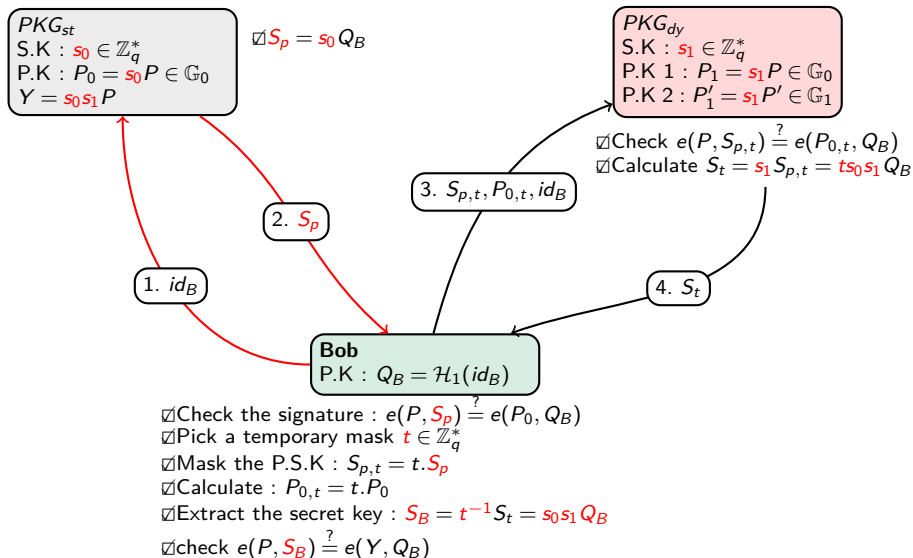


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$$\begin{array}{l}
 \text{PKG}_{st} \\
 \text{S.K} : s_0 \in \mathbb{Z}_q^* \\
 \text{P.K} : P_0 = s_0 P \in \mathbb{G}_0 \\
 Y = s_0 s_1 P
 \end{array}$$

$$\begin{array}{l}
 \text{PKG}_{dy} \\
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 \text{P.K 1} : P_1 = s_1 P \in \mathbb{G}_0 \\
 \text{P.K 2} : P'_1 = s_1 P' \in \mathbb{G}_1
 \end{array}$$

$$\begin{array}{l}
 \text{Bob} \\
 \text{P.K} : Q_B = \mathcal{H}_1(id_B) \\
 \text{S.K} : S_B = s_0 s_1 Q_B \\
 S_p = s_0 Q_B
 \end{array}$$

☐ Pick a temporary mask $t \in \mathbb{Z}_q^*$

FIGURE: The rekeying phase in IBE-2

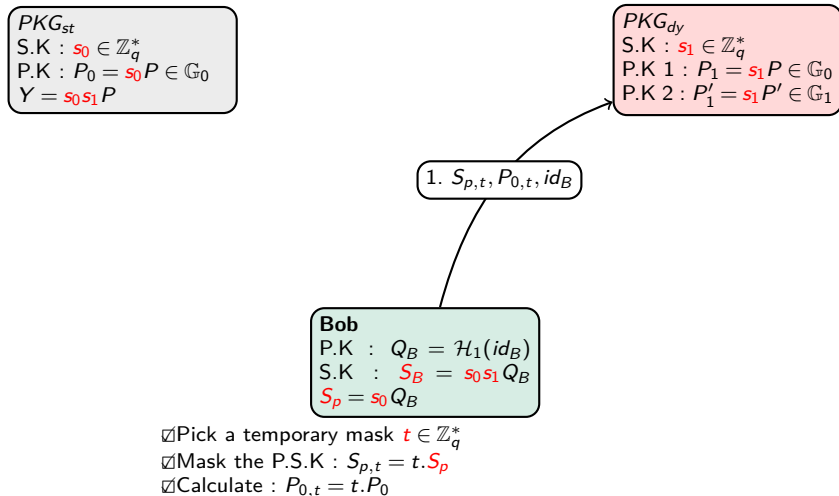


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\checkmark Check $e(P, S_{p,t}) \stackrel{?}{=} e(P_0, t, Q_B)$

1. $S_{p,t}, P_0, t, id_B$

Bob
 P.K : $Q_B = \mathcal{H}_1(id_B)$
 S.K : $S_B = s_0 s_1 Q_B$
 $S_p = s_0 Q_B$

- \checkmark Pick a temporary mask $t \in \mathbb{Z}_q^*$
- \checkmark Mask the P.S.K : $S_{p,t} = t \cdot S_p$
- \checkmark Calculate : $P_0, t = t \cdot P_0$

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1. $S_{p,t}, P_{0,t}, id_B$

- ✓ Check $e(P, S_{p,t}) \stackrel{?}{=} e(P_{0,t}, Q_B)$
- ✓ Calculate $S_t = s_1 S_{p,t} = t s_0 s_1 Q_B$

2. S_t

Bob
 P.K : $Q_B = \mathcal{H}_1(id_B)$
 S.K : $S_B = s_0 s_1 Q_B$
 $S_p = s_0 Q_B$

- ✓ Pick a temporary mask $t \in \mathbb{Z}_q^*$
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- ✓ Pick a temporary mask $t \in \mathbb{Z}_q^*$
- ✓ Mask the P.S.K : $S_{p,t} = t \cdot S_p$
- ✓ Calculate : $P_{0,t} = t \cdot P_0$
- ✓ Extract the secret key : $S_B = t^{-1} S_t = s_0 s_1 Q_B$
- ✓ check $e(P, S_B) \stackrel{?}{=} e(Y, Q_B)$

FIGURE: The rekeying phase in IBE-2

The revocation phase

We add an IRL (Identity Revocation List) that lists the identity of revoked entities. This list must respect those proprieties :

- Must be cleaned at each re-keying phase. Whence, we can revoke the entities in real time without increasing constantly the IRL ;
- The IRL is a reading only file for which only the security officer can add the revoked identities ;
- The IRL does not require to store keys ;
- The period T must be chosen in order to make the IRL nearly empty a most of the time, so it will not affect the network traffic fluidity.

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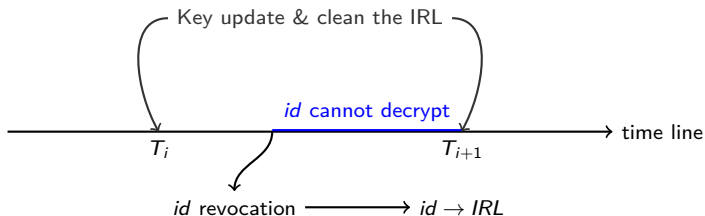


FIGURE: Real-time revocation in IBE-2

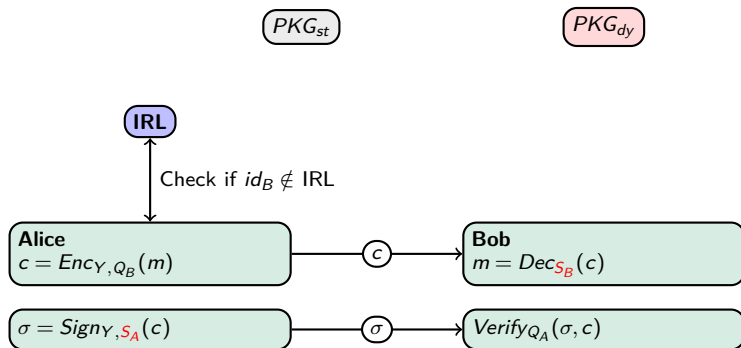
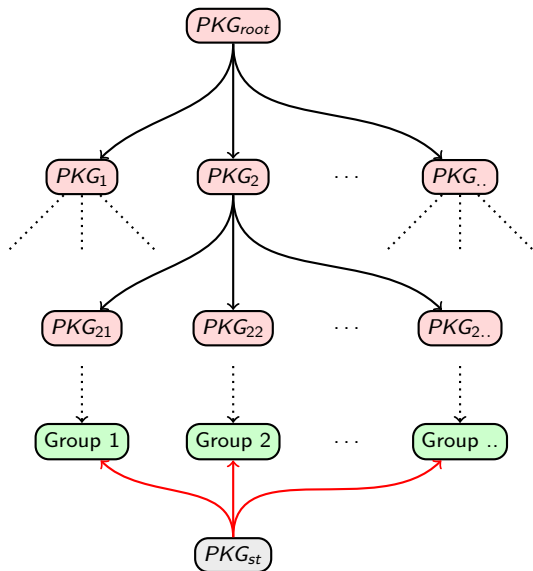


FIGURE: An authenticated encryption in IBE-2

Hierarchical IBE



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Conclusion :

- The security of the full system is not supported by one authority ;
- Neither PKG_{dy} or PKG_{st} can sign or encrypt instead of the user ;
- A flexible system designed to accept or reject the Key Recovery ;
- The communication with authorities is via a public channel ;
- Real time revocation, without increasing constantly the IRL ;
- The private key can be calculated in case of loss ;
- This infrastructure is fully compatible with the hierarchical model.

Thank you!

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